

K^+ Target Studies with Fluka – Extended

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I. Introduction

As an aid to developing a revised proposal for a possible experiment at Fermilab to obtain up to 1,000 events for the $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ decay [1], earlier Monte Carlo simulations [2] have been extended for stopping K^+ particles in a scintillating target.

The Tevatron that provided the beam for the original proposal is no longer available. The Main Injector will provide the beam in the revised proposal. To compensate for a lower beam intensity, a secondary K^+ beam with momentum greater than 550 MeV/ c may be needed. Beams of 600, 650, and 710 MeV/ c are considered in this report.

II. Components of the Study

Several of the degrading materials used in the previous study [2] were replaced with alternate, and more realistic, materials in the present study. Polyvinyltolulene (scintillator) requires very long lengths due to its low density, leading to substantial loss of beam upstream of the target. Synthetic diamond, although it seemed best in many regards, is not currently available in sufficient sizes or reasonable cost. Brass produces considerable photon and neutron backgrounds. In addition to BeO (density 3.0 g/cm³), consideration is given to SiO₂ (silica, quartz, glass) and Al₂O₃ (density 3.95 g/cm³). The density for SiO₂ was taken to be that of the crystal form, 2.65 g/cm³, although values closer to 2.2 g/cm³ might be more realistic. Aluminum oxide is often sold as a fine powder, but it can be packed into cylinders with nearly the full density. Blocks can also be cut from the mineral corundum (with minor impurities). Boron carbide (B₄C, density 2.52 g/cm³) was also considered briefly, and was found to be slightly less satisfactory than the other materials.

As for the original studies, the standalone Fluka Monte Carlo code [3] was used for all studies here. The most recent code release was used. It reproduced an earlier case within the accuracy of the random number sequencing.

Also as in the previous studies, the target was treated as a cylinder of solid scintillator (11 H to 10 C atoms) of radius 6 cm and length 1 meter. It was placed to start at $Z = 0$. All degraders, also 6 cm in radius, were placed at $Z < 0$, up to the target. The degrader thickness was estimated from an independent code so as to yield a K^+ momentum near 335 MeV/ c at the entrance to the target. The stopping peak was then approximately at 11-12 cm into the target.

III. Beamline and Logic

The beam profiles were obtained from the proposed beamline design. A beam file provided by Jaap Doornbos ('Jaap beam file') from the TRANSPORT code contained a list of X and

Y coordinates, their respective divergences, and momenta for rays computed at 1.5 meters from the end of the second quadrupole. The momenta are for a 500-MeV/ c beam, and were rescaled by the nominal beam momentum for other beams. The focal plane was taken to be $Z = 0$ in the setup. Unless otherwise stated, the beam profile was back-traced to a point 1 cm before any degrading materials.

The target and degrader were placed inside a cylindrical ‘sides’ region. An ‘end’ region was also placed at the far end of the target. A particle that crossed the boundary from the target or degrader into one of the regions was recorded as having ‘escaped.’

Within the target and degrader regions, stopped K^+ particles were identified as those that tracked until they had a momentum $p_K = 0$. Those that decayed in-flight along the way were identified with an internal code number that indicated the production of secondaries from decay, and which also had non-zero momentum. (The requirement of non-zero momentum was needed to prevent K^+ particles which stopped and then decayed from being double-counted.) Finally, K^+ particles that interacted with nuclei and disappeared were identified with a second internal code number for production of secondaries. The list of secondaries was scanned, and the K^+ was identified as ‘interacted’ if there was no such particle in the list. There are thus four classes of K^+ events: stopped, decayed, interacted, and escaped. The total number of kaons in these groups was about 99.5% of the beam.

IV. Yield Results

The numbers of stopped, decayed, interacted, and escaped K^+ , and the total number for 100,000 beam kaons are given in Table I for several combinations of beam momentum and degraders. These numbers are summed over the degrader and target regions. (Note that the 710-MeV/ c cases are included to give further illustration of the momentum dependence, and are *not* to be confused with the E949 setup.)

Several trends are evident from the table. First, materials with higher densities shorten the overall length, leading to fewer decayed or escaped kaons and to larger total numbers of stopped kaons. However, there is a cost in terms of more stopped and interacted kaons in the degraders. Heavier nuclei can also cause more multiple scatterings and produce larger backgrounds.

Second, higher beam momenta makes things worse: the total numbers of stopped K^+ are lower, and the numbers of interacted and escaped kaons are both higher. However, a higher beam flux at higher momenta may compensate in part.

Looking into the details, the results in the degrader and target were analyzed in terms of three sub-regions: (1) degrader, $Z < 0$; (2) a ‘tail’ region with $Z > 0$ but Z less than the start of a stopped K^+ peak; and (3) a ‘peak’ region for stopped K^+ above a starting point. The starting point of the ‘peak’ was estimated to be where the counts began to significantly rise above the preceding ‘tail’ region. The division into ‘tail’ and ‘peak’ sub-regions allows for the possibility that acceptance windows might be placed on the location of stopped kaons. Otherwise, the number of stopped K^+ in the target is the sum of the two sub-regions.

Table I: Stopped, decayed, interacted, and escaped K^+ particles for 100,000 beam kaons. The momentum has units MeV/ c , and the degrader thickness and ‘peak start’ positions are in cm.

| Momen. | Dgrdr Thick. | Peak Start | Stopped | Decayed | Interact | Escaped | Total |
|------------------------------------|--------------|------------|---------|---------|----------|---------|--------|
| <i>BeO</i> | | | | | | | |
| 500 | 11.5 | 7.0 | 81,410 | 9,018 | 4,175 | 4,898 | 99,501 |
| 550 | 16.4 | 6.0 | 77,017 | 9,330 | 5,886 | 7,260 | 99,493 |
| 600 | 21.8 | 6.0 | 71,605 | 9,696 | 7,726 | 10,547 | 99,547 |
| 650 | 27.7 | 5.0 | 65,822 | 9,837 | 9,846 | 14,049 | 99,554 |
| 710 | 35.4 | 3.0 | 58,512 | 10,164 | 12,467 | 18,503 | 99,646 |
| <i>Al₂O₃</i> | | | | | | | |
| 500 | 9.1 | 6.0 | 83,951 | 8,051 | 3,886 | 3,614 | 99,502 |
| 550 | 12.8 | 5.0 | 79,959 | 8,673 | 5,397 | 5,488 | 99,517 |
| 600 | 17.0 | 5.0 | 75,409 | 8,928 | 7,291 | 7,888 | 99,516 |
| 650 | 21.6 | 4.5 | 70,230 | 8,778 | 9,510 | 11,031 | 99,549 |
| 710 | 27.5 | 2.5 | 63,526 | 9,025 | 11,932 | 15,200 | 99,683 |
| <i>SiO₂</i> | | | | | | | |
| 500 | 13.2 | 6.0 | 80,724 | 9,422 | 3,721 | 5,617 | 99,484 |
| 550 | 18.8 | 5.0 | 75,781 | 9,921 | 5,350 | 8,452 | 99,504 |
| 600 | 24.9 | 5.5 | 69,335 | 10,658 | 7,173 | 12,327 | 99,493 |
| 650 | 31.6 | 4.0 | 63,085 | 10,604 | 9,059 | 16,823 | 99,571 |
| 710 | 40.0 | 3.0 | 54,996 | 10,753 | 11,456 | 22,380 | 99,585 |

The breakdown of stopped and decayed K^+ in the three sub-regions is shown in Table II. The breakdowns for the interacted kaons are not included as they account for less than 10% of the incident kaons and most of the interactions occur in the degraders. (About 75% of the interactions take place in the BeO degrader at 500 MeV/ c , and about 85% for the other materials; the fraction increases quickly with momentum to >95%.)

The loss of stopped K^+ between 500 and 650 MeV/ c in this table is larger than the corresponding loss of stopped K^+ in Table I. This extra loss is primarily related to more stops in the degrader. The 710-MeV/ c case makes the point clear. A minor benefit of a higher momentum is a comparative reduction of the ‘tail’ compared to the ‘peak’ subregion.

V. Common Starting Point

For all of the calculations above, the beam was started at 1 cm upstream of the degrader material for the case. As a result of different degrader thicknesses, these starting points are at different distances from the end of the last beamline quadrupole. There can be extra loss of flux due to decays and escaped particles in the space. Although the method used is considered to be best for assessing the intrinsic performance of the degraders, the results

Table II: Distribution of stopped and decayed K^+ particles in the degrader, ‘tail,’ and ‘peak’ sub-regions defined in the text.

| Momen. | Stopped K^+ | | | Decayed K^+ | | |
|------------------------------------|---------------|-------|--------|---------------|-------|-------|
| | Dgrdr | Tail | Peak | Dgrdr | Tail | Peak |
| <i>BeO</i> | | | | | | |
| 500 | 9,130 | 2,599 | 69,681 | 3,494 | 2,458 | 3,066 |
| 550 | 11,912 | 2,088 | 63,017 | 4,386 | 1,900 | 3,044 |
| 600 | 13,958 | 2,044 | 55,603 | 5,302 | 1,727 | 2,667 |
| 650 | 15,853 | 1,621 | 48,348 | 6,047 | 1,194 | 2,596 |
| 710 | 16,761 | 825 | 40,926 | 6,902 | 657 | 2,605 |
| <i>Al₂O₃</i> | | | | | | |
| 500 | 9,639 | 2,252 | 72,060 | 2,621 | 2,129 | 3,301 |
| 550 | 12,813 | 1,917 | 65,229 | 3,571 | 1,705 | 3,397 |
| 600 | 15,552 | 1,721 | 58,136 | 4,265 | 1,479 | 3,184 |
| 650 | 17,593 | 1,475 | 51,162 | 4,757 | 1,230 | 2,791 |
| 710 | 19,415 | 714 | 43,397 | 5,454 | 600 | 2,971 |
| <i>SiO₂</i> | | | | | | |
| 500 | 8,135 | 2,114 | 70,475 | 3,951 | 2,086 | 3,385 |
| 550 | 10,640 | 1,882 | 63,259 | 5,088 | 1,918 | 2,915 |
| 600 | 12,393 | 1,637 | 55,305 | 6,256 | 1,523 | 2,879 |
| 650 | 13,580 | 1,068 | 48,437 | 6,786 | 1,026 | 2,792 |
| 710 | 14,611 | 646 | 39,739 | 7,511 | 579 | 2,663 |

would not necessarily reflect the overall performance for the experiment.

The cases were thus rerun with a common beam starting point, independent of momentum. A value of 41 cm upstream of the target was used, as in the original report. The ‘sides’ region was extended to include the additional drift space. Results for some key numbers are shown in Table III.

As expected, the big changes (cf. Table II) are large increases in the number of decays in the beamline/degrader region, and some loss in the stopped K^+ peak. The numbers of interactions and escaped K^+ are not much changed. There is a loss of 5-7% of kaons in the target, whether stopped, decayed, or escaped. In addition, there is a beam survival factor of 0.75-0.80 between 500 and 650 MeV/c from the exit of the quadrupole to the common beamline point, depending on momentum.

VI. Secondaries

In addition to the kaons, production of secondary particles into the detector is also a matter of concern. Here, we consider all particles that ‘escaped’ into the outside region. Table IV lists the yields for the dominant particles. The results are organized by momentum to

Table III: Distributions of K^+ particles in various regions. The common beamline segment begins at $Z = -41$ cm.

| Momen. | Stopped K^+ | | Decayed K^+ | | Interact. BmLine | Escaped | | |
|------------------------------------|---------------|--------|---------------|-------|---------------------|---------|--------|--|
| | Dgrdr | Peak | Dgrdr | Peak | | Dgrdr | Target | |
| <i>BeO</i> | | | | | | | | |
| 500 | 8,452 | 64,421 | 7,676 | 2,793 | 3,428 | 1,521 | 2,889 | |
| 550 | 11,172 | 59,255 | 10,097 | 2,853 | 5,144 | 3,443 | 3,392 | |
| 600 | 13,433 | 53,303 | 9,276 | 2,527 | 7,133 | 6,235 | 3,534 | |
| 650 | 15,182 | 47,048 | 8,744 | 2,564 | 9,445 | 9,487 | 3,767 | |
| 710 | 16,545 | 40,667 | 7,789 | 2,550 | 12,177 | 16,060 | 3,756 | |
| <i>Al₂O₃</i> | | | | | | | | |
| 500 | 8,753 | 66,010 | 10,705 | 2,982 | 3,085 | 937 | 2,604 | |
| 550 | 12,093 | 60,836 | 9,804 | 3,202 | 4,680 | 2,053 | 3,269 | |
| 600 | 14,639 | 54,935 | 9,361 | 2,956 | 6,539 | 3,963 | 3,766 | |
| 650 | 16,868 | 49,173 | 8,680 | 2,658 | 8,775 | 6,391 | 4,074 | |
| 710 | 18,685 | 42,254 | 8,000 | 2,878 | 11,399 | 10,052 | 4,590 | |
| <i>SiO₂</i> | | | | | | | | |
| 500 | 7,527 | 65,387 | 7,108 | 3,143 | 2,960 | 2,045 | 3,164 | |
| 550 | 9,996 | 60,056 | 10,182 | 3,265 | 4,502 | 4,251 | 3,800 | |
| 600 | 11,928 | 53,626 | 9,312 | 2,707 | 6,428 | 7,169 | 4,504 | |
| 650 | 13,251 | 47,545 | 8,707 | 2,774 | 8,579 | 10,763 | 5,098 | |
| 710 | 14,573 | 39,502 | 7,840 | 2,688 | 11,125 | 15,267 | 6,173 | |

emphasize the comparisons between materials. The beam starting points for Table I are used.

In the table, no discrimination has been made on the number of daughter layers, or the origins of the particles. For example, π^0 s are not tracked, and the daughter photons are included in the γ column. Most of the μ^+ particles come from the decay of the K^+ . The fact that the μ^+ numbers are reduced in going to higher momenta reflects the reduction in the stopped and decayed K^+ .

The table does not include escaped K^0 and \bar{K}^0 particles. About 900, 1400, 2000, and 2500 K^0 were produced at 500, 550, 600, and 650 MeV/ c , respectively. The numbers are about 2/3 as large for \bar{K}^0 .

Many of the yields have, at most, modest dependence on beam momentum. But attention is drawn specifically to the γ and n numbers. Not only do they increase significantly with beam momentum, even for the same degrader material, they also depend on the material. The best material for photons is BeO, while SiO₂ is best for neutrons. Aluminum oxide is best for protons, π^- , and K^+ , but it is the worst for e^+ , photons, and neutrons.

Table IV: Yields of the dominant particles that ‘escape’ from the degrader and target into a detector region.

| Mom. | Dgrdr | p | e^+ | e^- | γ | n | μ^+ | π^+ | π^- | K^+ |
|------|-------|------|--------|--------|----------|--------|---------|---------|---------|--------|
| 500 | BeO | 1174 | 15,476 | 19,109 | 133,718 | 21,821 | 57,722 | 18,604 | 1604 | 4,898 |
| 500 | SiO2 | 1006 | 15,809 | 19,073 | 147,397 | 18,724 | 57,917 | 18,733 | 1600 | 5,617 |
| 500 | Al2O3 | 996 | 15,838 | 19,004 | 154,959 | 21,815 | 58,291 | 18,648 | 1434 | 3,614 |
| 550 | BeO | 1182 | 15,925 | 18,594 | 142,147 | 28,064 | 55,319 | 18,086 | 1961 | 7,260 |
| 550 | SiO2 | 1189 | 16,599 | 19,035 | 164,426 | 23,490 | 55,224 | 18,116 | 1985 | 8,452 |
| 550 | Al2O3 | 1034 | 17,082 | 19,313 | 180,325 | 27,901 | 55,938 | 17,935 | 1772 | 5,488 |
| 600 | BeO | 1346 | 15,755 | 17,824 | 147,986 | 33,916 | 52,180 | 17,366 | 2357 | 10,547 |
| 600 | SiO2 | 1398 | 17,086 | 18,155 | 181,723 | 28,440 | 51,5140 | 17,689 | 2323 | 12,327 |
| 600 | Al2O3 | 1110 | 17,413 | 18,860 | 201,247 | 35,150 | 53,224 | 17,567 | 2101 | 7,888 |
| 650 | BeO | 1834 | 15,835 | 17,225 | 158,701 | 41,797 | 48,204 | 16,714 | 2705 | 14,049 |
| 650 | SiO2 | 2021 | 17,145 | 17,381 | 194,714 | 34,180 | 47,526 | 16,816 | 2741 | 16,823 |
| 650 | Al2O3 | 1339 | 18,075 | 17,910 | 224,178 | 43,982 | 50,260 | 16,388 | 2472 | 11,031 |
| 710 | BeO | 3039 | 16,503 | 16,243 | 170,558 | 50,017 | 43,780 | 16,034 | 3355 | 18,503 |
| 710 | SiO2 | 3512 | 17,540 | 16,205 | 209,723 | 41,108 | 41,108 | 16,115 | 3329 | 22,380 |
| 710 | Al2O3 | 1768 | 18,929 | 17,634 | 249,733 | 53,965 | 45,699 | 15,776 | 2936 | 15,200 |

VII. Conclusions

The stopped K^+ numbers for the ‘peak’ sub-region in Table II (divided by 100,000) are good estimates of the stopping efficiencies for the $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ experiment design, including all stopped K^+ in the target. The yield is reduced by about 25% in raising the beam momentum from 550 to 650 MeV/ c , at the expense of stopped and decayed K^+ in the degrader.

Because trigger scintillators and beam monitors may also be needed upstream, the net stopping efficiency might be slightly lower but still quite good. Due to its high density, Al₂O₃ appears to be best for reducing the degrader length, but it also produces higher backgrounds. If the latter are not critical issues, it might be the best material. Otherwise, BeO appears to be a satisfactory choice.

References

- [1] Fermilab proposal P996.
- [2] J.R. Comfort, “ K^+ Target Studies with Fluka,” Fermilab DocDB Kaon Physics 718 (2009).
- [3] Fluka Monte Carlo code. See <http://www.fluka.org/fluka.php> and references therein.